## A Note on Human Development Indices with Income Equalities

SK Mishra<br>Department of Economics North-Eastern Hill University Shillong (India)

Introduction: Sarker et al. (2006) in their paper argued that Human Development Index (HDI) should include income equality measures (EQ) also in addition to the three measures of life expectancy (LE), education (ED) and per capita gross domestic product at the purchasing power parity with the US $\$(\mathrm{PCI})$, conventionally incorporated into it. They computed the per capita income distribution-adjusted composite index (DAPCHDI) of human development and showed that the ranking of countries on the basis of this type of HDI (that includes income distribution as one of the component indices) differed substantially from the ranking calculated in the Human Development Reports (HDR) of UNDP (published annually). They suggested, therefore, that within-country income distribution should be given its due importance in international comparison of countries.

Sarker et al. used data on life expectancy, educational index and per capita income from the Human Development Report of UNDP for 2004. From the information on Gini coefficients of income distribution available in the HDR for various years they also constructed an index to measure equality in distribution of per capita income. They used the Gini coefficients data over a span of 13 years (1990-2002). Under the constraints of data availability on income distribution, they chose 125 countries for construction of distribution-augmented HDI. The indices were subjected to the principal component analysis (PCA) and two composite indices of Human Development, the one (PCHDI) without incorporating equality index and the other (DAPCHDI) with its inclusion were obtained. They noted, among other points, the following:

- Against the equal HDR weights for every index ( $1 / 3 \approx 0.333$ ), the principal component weights for life expectancy, education and per capita income in the PCHDI were $0.36,0.32$ and 0.32 respectively. These weights were $0.30,0.25$ and 0.25 for the DAPCHDI. Since the latter also includes the equality index, the residual ( 0.20 ) weight was assumed by this additional variable. These weights sum up to unity.
- Due to change in weights assigned to different indices to make their linear aggregate (the composite index of HDI), the ranks of different countries in PCHDI and DAPCHDI were notably different.

The Present Study: Our objective here is twofold. First, we re-compute the DAPCHDI with the data given by Sarker et al. in their paper to compare our composite index with theirs. The HDR-2005 or the HDR-2006 adds little to the HDR-2004 database. Secondly, we compute a slightly different DAPCHDI by a new method, which, unlike the principal component analysis that aims at maximizing the sum of squared coefficients of correlation between the composite index and the constituent variables, maximizes, instead, the sum of absolute coefficients of correlation between the composite index and the constituent variables. We call them $\mathrm{NHDI}_{2}$ and $\mathrm{NHDI}_{1}$ respectively.

Haq (2003) noted that there is no a priori rationale for assigning different weights to different constituent indices. Each dimension of development is important, but the importance of each dimension may be different for developed and developing countries. Hence, he pleaded for equal weights on the principle of insufficient reason to discriminate among the constituent indices. In a hurry to abandon income as a sole measure of development, the protagonists of human development resorted to extreme pragmatism. On the other hand, the PCA, a blindly empiricist method, has a tendency to undermine poorly correlated variables and instead favor highly correlated variables to make a composite index (Mishra, 2007-a and 2007-b). A comparison of the principal component index with the one constructed by maximizing the sum of absolute correlation coefficients has revealed that the latter is an inclusive index (giving due weights to poorly correlated variable too) while the principal component index is largely elitist, favoring highly correlated variables and undermining the poorly correlated ones (Mishra, 2007-c).

A Formal Description: It has been mentioned that the PCA makes a composite index such that the sum of squared coefficients of correlation between the composite index and the constituent variables is maximized. On the other hand, our new (inclusive) method maximizes the sum of absolute coefficients of correlation between the composite index and the constituent variables. Formally, if $I=X w=\sum_{j=1}^{m} w_{j} x_{i j} ; i=1,2, \ldots, n$ is the composite index, $x_{j} ; j=1,2, \ldots, m$ are the constituent variables (such as the life expectancy index, educational index, etc) and $r\left(I, x_{j}\right)$ is the coefficient of correlation between $I$ and $x_{j}$ then,
(1). $I$ (PCA) is obtained by maximizing $\sum_{j=1}^{m} r^{2}\left(I, x_{j}\right)$ or $\sum_{j=1}^{m}\left|r\left(I, x_{j}\right)\right|^{2}$ or $\left[\sum_{j=1}^{m}\left|r\left(I, x_{j}\right)\right|^{2}\right]^{1 / 2}$
(2). I (new method) is obtained by maximizing $\sum_{j=1}^{m}\left|r\left(I, x_{j}\right)\right|$

These measures relate to the Minkowski norm, $\mathrm{L}_{\mathrm{p}}$, for $\mathrm{p}=2$ and $\mathrm{p}=1$ respectively. The $I$ (PCA) may be obtained by maximizing the above measure directly by some suitable method of non-linear optimization or by the traditional method (finding largest eigenvalue and the associated eigenvector of the correlation matrix of constituent variables, etc). However, $I$ (new method) must be obtained by direct maximization.

Findings: We have maximized the quantities directly (Mishra, 2007-d) by the Differential Evolution method of global optimization to obtain $I$ (PCA) and $I$ (new method) from the four indices, namely life expectancy (LE), education (ED), per capita income (PCI) and equality index (EQ). The data for 125 countries, given by Sarker et al. in their paper, are reproduced in Table-4 here. We also reproduce the HDR-2004 ranks $\left(\mathrm{R}_{1}\right)$, PCHDI ranks ( $\mathrm{R}_{2}$ ) and values as well as the DAPCHDI ranks $\left(\mathrm{R}_{3}\right)$ and values obtained by Sarker et al. It may further be noted that computation of $I$ (PCA) by the traditional method gives the same correlation coefficients (loadings) to variables (LE, $\mathrm{ED}, \mathrm{PCI}$ and EQ) as does the direct optimization method.

The HDI indices computed by us are $\mathrm{NHDI}_{2}$ (principal component) and $\mathrm{NHDI}_{1}$ (new method) and the ranks obtained by different countries are $R_{4}$ and $R_{5}$ respectively.

These HDI indices too are presented in Table-4. Note that ranks are based on more accurate $\mathrm{NHDI}_{2}$ and $\mathrm{NHDI}_{1}$ figures than what are presented in the Table-4.

In our analysis, the constituent indices of HDI obtain different weights and are differently correlated with their composite HDI indices. These weights and correlation coefficients are given in Table-1 and Table-2 respectively.

| Table-1: Weights assigned to the Constituent Indices by Different Methods |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Indices | LE | ED | PCI | EQ |
| DAPCHDI | 0.30 | 0.25 | 0.25 | 0.20 |
| NHDI $_{2}$ | 0.270909751 | 0.275588551 | 0.289481714 | 0.164019853 |
| NHDI $_{1}$ | 0.239643184 | 0.258695275 | 0.265657700 | 0.236003815 |


| Table-2: Correlation of Composite HDI Indices with Different Constituent Indices |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Index | LE | ED | PCI | EQ | SAR | SSR |
| NHDI $_{2}$ | 0.923635411 | 0.870389039 | 0.890306269 | 0.567829911 | 3.25216063 | 2.72575551 |
| NHDI $_{1}$ | 0.914036295 | 0.845974366 | 0.865869176 | 0.639601336 | 3.26548117 | 2.70995428 |
| SAR=Sum of Absolute correlation coefficients; SSR=Sum of Squared correlation coefficients |  |  |  |  |  |  |

It may be noted that $\mathrm{NHDI}_{1}$ trades off SSR only slightly to assign higher weights to EQ index. In exchange, the weights of LE, ED and PCI are reduced. Overall, $\mathrm{NHDI}_{1}$ weights are more egalitarian than the $\mathrm{NHDI}_{2}$ weights. Finally, in the Table-3 below we present the matrix of correlation coefficients (based on figures in Table-4) among and across different ranks and composite HDI measures.

| Table-3: | lation | Matrix | Differen | Rank | nd HDI | dices ob | ined by | ferent | ds |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ranks/ HDI Indices | Ranks obtained by Different Methods |  |  |  |  | HDI Indices obtained by Different Methods |  |  |  |
|  | R1 | R2 | R3 | R4 | R5 | PCHDI | $\begin{gathered} \hline \text { DA } \\ \text { PCHDI } \end{gathered}$ | $\mathrm{NHDI}_{2}$ | $\mathrm{NHDI}_{1}$ |
| R1 | 1.00000 | 0.99969 | 0.96199 | 0.97512 | 0.95372 | -0.97103 | -0.95206 | -0.96446 | -0.94855 |
| R2 | 0.99969 | 1.00000 | 0.96289 | 0.97568 | 0.95443 | -0.97105 | -0.95320 | -0.96515 | -0.94960 |
| R3 | 0.96199 | 0.96289 | 1.00000 | 0.99736 | 0.99878 | -0.94587 | -0.98259 | -0.98089 | -0.98573 |
| R4 | 0.97512 | 0.97568 | 0.99736 | 1.00000 | 0.99478 | -0.95589 | -0.98075 | -0.98235 | -0.98284 |
| R5 | 0.95372 | 0.95443 | 0.99878 | 0.99478 | 1.00000 | -0.93923 | -0.98202 | -0.97900 | -0.98633 |
| PCHDI | -0.97103 | -0.97105 | -0.94587 | -0.95589 | -0.93923 | 1.00000 | 0.97141 | 0.98302 | 0.96251 |
| DAPCHDI | -0.95206 | -0.95320 | -0.98259 | -0.98075 | -0.98202 | 0.97141 | 1.00000 | 0.99783 | 0.99865 |
| $\mathrm{NHDI}_{2}$ | -0.96446 | -0.96515 | -0.98089 | -0.98235 | -0.97900 | 0.98302 | 0.99783 | 1.00000 | 0.99569 |
| $\mathrm{NHDI}_{1}$ | -0.94855 | -0.94960 | -0.98573 | -0.98284 | -0.98633 | 0.96251 | 0.99865 | 0.99569 | 1.00000 |

Concluding Remarks: The Human Development Reports assign subjective (or arbitrary) weights to indices of life expectancy, education, and income. Inclusion of equality index to HDI naturally raises the question as to the weight to be assigned to it. It is also required to reduce the weights assigned to other indices. An attempt may be made to obtain weights by the principal component analysis. However, the principal component analysis has a tendency to undermine the variables with weaker correlation coefficients. It may be elitist in favoring the highly correlated indices. Variance or explanatory power of a composite index cannot be the sole guide to assign weights. Representation of individual indices in the composite HDI also matters. The HDR has taken an extreme stand of assigning equal weights to all indices and suffers from an excessive bias to pragmatism. However, the new method of obtaining weights and constructing an HDI
suggested by us is inclusive in nature, which takes care of weakly correlated indices also and gives them proper representation in the composite Human Development Index.

Table-4: Composite Indices of Human Development in Select Countries obtained by Different Methods

| Select Countries | Ranks by Different Methods |  |  |  |  | Human Development Indices: Different Aspects |  |  |  | Composite Indices of HDI |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | R1 | R2 | R3 | R4 | R5 | LE | ED | PCl | EQ | $\begin{aligned} & \text { PC } \\ & \text { HDI } \\ & \hline \end{aligned}$ | $\begin{gathered} \hline \text { DAPC } \\ \text { HDI } \end{gathered}$ | New Indices |  |
|  |  |  |  |  |  |  |  |  |  |  |  | $\mathrm{NHDl}_{2}$ | NHDI ${ }_{1}$ |
| Norway | 1 | 1 | 1 | 1 | 1 | 0.90 | 0.99 | 0.99 | 0.96 | 0.96 | 0.96 | 0.96 | 0.96 |
| Sweden | 2 | 2 | 2 | 2 | 2 | 0.92 | 0.99 | 0.93 | 0.98 | 0.95 | 0.95 | 0.95 | 0.95 |
| Canada | 3 | 3 | 11 | 11 | 11 | 0.90 | 0.98 | 0.95 | 0.81 | 0.94 | 0.91 | 0.92 | 0.91 |
| Netherlands | 4 | 6 | 10 | 8 | 10 | 0.89 | 0.99 | 0.95 | 0.82 | 0.94 | 0.92 | 0.92 | 0.92 |
| Australia | 5 | 4 | 14 | 13 | 14 | 0.90 | 0.99 | 0.94 | 0.76 | 0.94 | 0.90 | 0.91 | 0.90 |
| Belgium | 6 | 5 | 3 | 3 | 3 | 0.90 | 0.99 | 0.94 | 0.98 | 0.94 | 0.95 | 0.95 | 0.95 |
| United_States | 7 | 7 | 23 | 20 | 26 | 0.87 | 0.97 | 0.98 | 0.64 | 0.94 | 0.88 | 0.89 | 0.87 |
| Japan | 8 | 8 | 4 | 4 | 5 | 0.94 | 0.94 | 0.93 | 0.98 | 0.94 | 0.95 | 0.94 | 0.95 |
| Luxembourg | 9 | 10 | 9 | 10 | 9 | 0.89 | 0.91 | 1.00 | 0.86 | 0.93 | 0.92 | 0.92 | 0.92 |
| Ireland | 10 | 14 | 18 | 16 | 17 | 0.86 | 0.96 | 0.98 | 0.75 | 0.93 | 0.89 | 0.90 | 0.89 |
| Switzerland | 11 | 9 | 12 | 12 | 12 | 0.90 | 0.95 | 0.95 | 0.81 | 0.93 | 0.91 | 0.91 | 0.90 |
| Austria | 12 | 11 | 8 | 9 | 8 | 0.89 | 0.96 | 0.95 | 0.87 | 0.93 | 0.92 | 0.92 | 0.92 |
| United_Kingdom | 13 | 12 | 17 | 17 | 19 | 0.88 | 0.99 | 0.93 | 0.74 | 0.93 | 0.89 | 0.90 | 0.89 |
| Finland | 14 | 13 | 6 | 6 | 6 | 0.88 | 0.99 | 0.93 | 0.94 | 0.93 | 0.93 | 0.93 | 0.94 |
| Denmark | 15 | 15 | 5 | 5 | 4 | 0.86 | 0.98 | 0.96 | 0.99 | 0.93 | 0.94 | 0.94 | 0.95 |
| France | 16 | 16 | 13 | 14 | 13 | 0.90 | 0.96 | 0.93 | 0.81 | 0.93 | 0.91 | 0.91 | 0.90 |
| New_Zealand | 17 | 17 | 19 | 19 | 21 | 0.89 | 0.99 | 0.90 | 0.74 | 0.93 | 0.89 | 0.90 | 0.88 |
| Germany | 18 | 18 | 7 | 7 | 7 | 0.89 | 0.95 | 0.94 | 0.91 | 0.93 | 0.92 | 0.92 | 0.92 |
| Spain | 19 | 19 | 15 | 15 | 15 | 0.90 | 0.97 | 0.90 | 0.82 | 0.92 | 0.90 | 0.91 | 0.90 |
| Italy | 20 | 20 | 21 | 21 | 23 | 0.89 | 0.93 | 0.93 | 0.74 | 0.92 | 0.88 | 0.89 | 0.88 |
| Israel | 21 | 21 | 24 | 23 | 24 | 0.90 | 0.94 | 0.88 | 0.76 | 0.91 | 0.88 | 0.88 | 0.87 |
| Singapore | 22 | 23 | 30 | 29 | 32 | 0.88 | 0.91 | 0.92 | 0.61 | 0.90 | 0.84 | 0.86 | 0.83 |
| Greece | 23 | 22 | 26 | 25 | 27 | 0.89 | 0.95 | 0.87 | 0.76 | 0.90 | 0.87 | 0.88 | 0.87 |
| Hong_Kong_China_(SAR) | 24 | 24 | 32 | 30 | 33 | 0.91 | 0.86 | 0.93 | 0.59 | 0.90 | 0.84 | 0.85 | 0.83 |
| Portugal | 25 | 25 | 28 | 27 | 28 | 0.85 | 0.97 | 0.87 | 0.69 | 0.89 | 0.85 | 0.86 | 0.85 |
| Slovenia | 26 | 26 | 16 | 18 | 16 | 0.85 | 0.96 | 0.87 | 0.91 | 0.89 | 0.89 | 0.90 | 0.90 |
| Korea_Rep_of | 27 | 27 | 22 | 24 | 22 | 0.84 | 0.97 | 0.86 | 0.84 | 0.89 | 0.88 | 0.88 | 0.88 |
| Czech_Republic | 28 | 28 | 20 | 22 | 18 | 0.84 | 0.92 | 0.84 | 0.97 | 0.87 | 0.89 | 0.88 | 0.89 |
| Argentina | 29 | 29 | 47 | 45 | 49 | 0.82 | 0.96 | 0.78 | 0.40 | 0.85 | 0.76 | 0.78 | 0.75 |
| Estonia | 30 | 30 | 34 | 34 | 34 | 0.78 | 0.98 | 0.80 | 0.72 | 0.85 | 0.82 | 0.83 | 0.82 |
| Poland | 31 | 31 | 29 | 31 | 29 | 0.81 | 0.96 | 0.78 | 0.84 | 0.85 | 0.85 | 0.85 | 0.85 |
| Hungary | 32 | 32 | 25 | 26 | 20 | 0.78 | 0.95 | 0.82 | 1.00 | 0.85 | 0.87 | 0.87 | 0.89 |
| Slovakia | 33 | 33 | 27 | 28 | 25 | 0.81 | 0.91 | 0.81 | 0.96 | 0.84 | 0.87 | 0.86 | 0.87 |
| Lithuania | 34 | 35 | 33 | 33 | 31 | 0.79 | 0.96 | 0.77 | 0.83 | 0.84 | 0.84 | 0.84 | 0.84 |
| Chile | 35 | 34 | 60 | 49 | 64 | 0.85 | 0.90 | 0.77 | 0.30 | 0.84 | 0.73 | 0.75 | 0.71 |
| Uruguay | 36 | 36 | 43 | 43 | 44 | 0.84 | 0.94 | 0.73 | 0.56 | 0.84 | 0.78 | 0.79 | 0.77 |
| Costa_Rica | 37 | 37 | 45 | 44 | 47 | 0.88 | 0.87 | 0.75 | 0.52 | 0.84 | 0.77 | 0.78 | 0.76 |
| Croatia | 38 | 38 | 31 | 32 | 30 | 0.82 | 0.90 | 0.77 | 0.89 | 0.83 | 0.84 | 0.84 | 0.84 |
| Latvia | 39 | 39 | 36 | 35 | 35 | 0.76 | 0.95 | 0.75 | 0.82 | 0.82 | 0.82 | 0.82 | 0.82 |
| Mexico | 40 | 40 | 66 | 63 | 72 | 0.81 | 0.85 | 0.75 | 0.35 | 0.80 | 0.71 | 0.73 | 0.70 |
| Trinidad_and_Tobago | 41 | 41 | 46 | 47 | 45 | 0.77 | 0.87 | 0.76 | 0.65 | 0.80 | 0.77 | 0.77 | 0.76 |
| Bulgaria | 42 | 42 | 40 | 39 | 40 | 0.77 | 0.91 | 0.71 | 0.83 | 0.80 | 0.80 | 0.80 | 0.80 |
| Malaysia | 43 | 45 | 63 | 58 | 63 | 0.80 | 0.83 | 0.75 | 0.46 | 0.79 | 0.73 | 0.74 | 0.71 |
| Russian_Federation | 44 | 46 | 57 | 48 | 55 | 0.69 | 0.95 | 0.74 | 0.54 | 0.79 | 0.74 | 0.75 | 0.74 |
| Macedonia_TFYR | 45 | 44 | 35 | 36 | 36 | 0.81 | 0.87 | 0.70 | 0.91 | 0.79 | 0.82 | 0.81 | 0.82 |


| Panama | 46 | 43 | 73 | 67 | 79 | 0.83 | 0.86 | 0.69 | 0.31 | 0.79 | 0.70 | 0.71 | 0.68 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Belarus | 47 | 47 | 39 | 40 | 39 | 0.75 | 0.95 | 0.67 | 0.86 | 0.79 | 0.80 | 0.80 | 0.81 |
| Albania | 48 | 48 | 38 | 38 | 38 | 0.81 | 0.89 | 0.65 | 0.91 | 0.78 | 0.81 | 0.80 | 0.81 |
| Bosnia_and_Herzegovi | 49 | 49 | 37 | 37 | 37 | 0.82 | 0.84 | 0.68 | 0.95 | 0.78 | 0.82 | 0.81 | 0.82 |
| Venezuela | 50 | 50 | 64 | 65 | 66 | 0.81 | 0.86 | 0.67 | 0.47 | 0.78 | 0.72 | 0.73 | 0.71 |
| Romania | 51 | 51 | 42 | 41 | 42 | 0.76 | 0.88 | 0.70 | 0.87 | 0.78 | 0.80 | 0.79 | 0.80 |
| Ukraine | 52 | 53 | 41 | 42 | 41 | 0.74 | 0.94 | 0.65 | 0.89 | 0.78 | 0.80 | 0.79 | 0.80 |
| Saint_Lucia | 53 | 52 | 54 | 51 | 57 | 0.79 | 0.88 | 0.66 | 0.60 | 0.78 | 0.74 | 0.75 | 0.73 |
| Brazil | 54 | 54 | 81 | 78 | 81 | 0.72 | 0.88 | 0.73 | 0.25 | 0.77 | 0.67 | 0.69 | 0.65 |
| Colombia | 55 | 55 | 80 | 77 | 80 | 0.78 | 0.84 | 0.69 | 0.29 | 0.77 | 0.67 | 0.69 | 0.66 |
| Thailand | 56 | 56 | 58 | 57 | 59 | 0.74 | 0.86 | 0.71 | 0.59 | 0.77 | 0.73 | 0.74 | 0.73 |
| Kazakhstan | 57 | 57 | 44 | 46 | 43 | 0.69 | 0.93 | 0.68 | 0.84 | 0.76 | 0.78 | 0.78 | 0.78 |
| Jamaica | 58 | 58 | 49 | 50 | 51 | 0.84 | 0.83 | 0.61 | 0.70 | 0.76 | 0.75 | 0.75 | 0.74 |
| Armenia | 59 | 59 | 52 | 54 | 54 | 0.79 | 0.90 | 0.57 | 0.70 | 0.75 | 0.75 | 0.74 | 0.74 |
| Philippines | 60 | 60 | 67 | 66 | 68 | 0.75 | 0.89 | 0.62 | 0.53 | 0.75 | 0.71 | 0.71 | 0.70 |
| Turkmenistan | 61 | 61 | 62 | 61 | 60 | 0.70 | 0.93 | 0.63 | 0.64 | 0.75 | 0.73 | 0.73 | 0.73 |
| Paraguay | 62 | 62 | 82 | 81 | 85 | 0.76 | 0.85 | 0.64 | 0.30 | 0.75 | 0.66 | 0.67 | 0.64 |
| Peru | 63 | 64 | 78 | 74 | 78 | 0.74 | 0.86 | 0.65 | 0.45 | 0.75 | 0.69 | 0.70 | 0.68 |
| Turkey | 64 | 63 | 59 | 60 | 58 | 0.76 | 0.80 | 0.69 | 0.66 | 0.75 | 0.73 | 0.73 | 0.73 |
| Azerbaijan | 65 | 65 | 51 | 56 | 53 | 0.78 | 0.88 | 0.58 | 0.73 | 0.75 | 0.75 | 0.74 | 0.74 |
| Jordan | 66 | 66 | 53 | 53 | 50 | 0.76 | 0.86 | 0.62 | 0.74 | 0.75 | 0.75 | 0.74 | 0.74 |
| Tunisia | 67 | 67 | 61 | 62 | 61 | 0.79 | 0.74 | 0.70 | 0.66 | 0.75 | 0.73 | 0.73 | 0.72 |
| China | 68 | 68 | 69 | 69 | 69 | 0.76 | 0.83 | 0.64 | 0.56 | 0.74 | 0.71 | 0.71 | 0.70 |
| Georgia | 69 | 69 | 55 | 59 | 56 | 0.81 | 0.89 | 0.52 | 0.73 | 0.74 | 0.74 | 0.73 | 0.73 |
| Dominican_Republic | 70 | 71 | 76 | 73 | 76 | 0.70 | 0.82 | 0.70 | 0.50 | 0.74 | 0.69 | 0.70 | 0.68 |
| Sri_Lanka | 71 | 70 | 50 | 52 | 48 | 0.79 | 0.83 | 0.60 | 0.78 | 0.74 | 0.75 | 0.74 | 0.75 |
| Ecuador | 72 | 72 | 70 | 70 | 71 | 0.76 | 0.85 | 0.60 | 0.58 | 0.74 | 0.71 | 0.71 | 0.70 |
| Iran_Islamic_Rep_of | 73 | 73 | 71 | 71 | 70 | 0.75 | 0.74 | 0.70 | 0.60 | 0.73 | 0.70 | 0.71 | 0.70 |
| El_Salvador | 74 | 74 | 83 | 83 | 87 | 0.76 | 0.75 | 0.65 | 0.38 | 0.72 | 0.65 | 0.66 | 0.64 |
| Guyana | 75 | 75 | 77 | 75 | 75 | 0.64 | 0.89 | 0.63 | 0.59 | 0.72 | 0.69 | 0.70 | 0.69 |
| Uzbekistan | 76 | 76 | 48 | 55 | 46 | 0.74 | 0.91 | 0.47 | 0.94 | 0.71 | 0.76 | 0.74 | 0.76 |
| Algeria | 77 | 77 | 65 | 68 | 62 | 0.74 | 0.69 | 0.68 | 0.76 | 0.70 | 0.72 | 0.71 | 0.72 |
| Kyrgyzstan | 78 | 78 | 56 | 64 | 52 | 0.72 | 0.92 | 0.46 | 0.89 | 0.70 | 0.74 | 0.73 | 0.74 |
| Indonesia | 79 | 80 | 68 | 72 | 65 | 0.69 | 0.80 | 0.58 | 0.78 | 0.69 | 0.71 | 0.70 | 0.71 |
| Viet_Nam | 80 | 79 | 72 | 76 | 67 | 0.73 | 0.82 | 0.52 | 0.74 | 0.69 | 0.70 | 0.70 | 0.70 |
| Moldova_Rep_of | 81 | 81 | 74 | 79 | 73 | 0.73 | 0.87 | 0.45 | 0.74 | 0.69 | 0.70 | 0.69 | 0.69 |
| Bolivia | 82 | 82 | 84 | 84 | 82 | 0.64 | 0.86 | 0.53 | 0.56 | 0.68 | 0.65 | 0.66 | 0.65 |
| Honduras | 83 | 84 | 91 | 90 | 90 | 0.73 | 0.74 | 0.54 | 0.34 | 0.67 | 0.61 | 0.61 | 0.59 |
| Tajikistan | 84 | 85 | 75 | 80 | 74 | 0.73 | 0.90 | 0.38 | 0.77 | 0.67 | 0.69 | 0.68 | 0.69 |
| Nicaragua | 85 | 83 | 90 | 91 | 91 | 0.74 | 0.73 | 0.54 | 0.34 | 0.67 | 0.61 | 0.61 | 0.59 |
| Mongolia | 86 | 86 | 85 | 85 | 84 | 0.64 | 0.89 | 0.47 | 0.57 | 0.67 | 0.65 | 0.65 | 0.64 |
| South_Africa | 87 | 88 | 94 | 92 | 95 | 0.40 | 0.83 | 0.77 | 0.25 | 0.66 | 0.57 | 0.60 | 0.57 |
| Egypt | 88 | 87 | 79 | 82 | 77 | 0.73 | 0.62 | 0.61 | 0.78 | 0.66 | 0.68 | 0.67 | 0.68 |
| Guatemala | 89 | 89 | 89 | 88 | 89 | 0.68 | 0.65 | 0.62 | 0.48 | 0.65 | 0.62 | 0.62 | 0.61 |
| Morocco | 90 | 90 | 87 | 87 | 88 | 0.72 | 0.53 | 0.61 | 0.67 | 0.62 | 0.64 | 0.63 | 0.63 |
| Namibia | 91 | 91 | 108 | 103 | 111 | 0.34 | 0.79 | 0.69 | 0.00 | 0.60 | 0.47 | 0.51 | 0.47 |
| India | 92 | 92 | 86 | 86 | 83 | 0.64 | 0.59 | 0.55 | 0.82 | 0.60 | 0.64 | 0.63 | 0.65 |
| Botswana | 93 | 93 | 105 | 100 | 105 | 0.27 | 0.76 | 0.73 | 0.17 | 0.57 | 0.49 | 0.52 | 0.50 |
| Ghana | 94 | 94 | 88 | 89 | 86 | 0.55 | 0.65 | 0.51 | 0.87 | 0.57 | 0.63 | 0.62 | 0.64 |
| Cambodia | 95 | 95 | 92 | 93 | 92 | 0.54 | 0.66 | 0.50 | 0.65 | 0.57 | 0.58 | 0.58 | 0.59 |
| Papua_New_Guinea | 96 | 96 | 99 | 99 | 101 | 0.54 | 0.57 | 0.52 | 0.43 | 0.54 | 0.52 | 0.52 | 0.52 |
| Lao_People's_Dem_Rep | 97 | 97 | 95 | 94 | 94 | 0.49 | 0.64 | 0.47 | 0.72 | 0.53 | 0.57 | 0.56 | 0.58 |
| Swaziland | 98 | 100 | 113 | 107 | 113 | 0.18 | 0.74 | 0.64 | 0.21 | 0.51 | 0.44 | 0.47 | 0.45 |
| Bangladesh | 99 | 98 | 93 | 95 | 93 | 0.60 | 0.45 | 0.47 | 0.83 | 0.51 | 0.58 | 0.56 | 0.58 |


| Nepal | 100 | 99 | 97 | 97 | 97 | 0.58 | 0.50 | 0.44 | 0.73 | 0.51 | 0.55 | 0.54 | 0.56 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cameroon | 101 | 102 | 102 | 102 | 100 | 0.36 | 0.64 | 0.50 | 0.56 | 0.49 | 0.51 | 0.51 | 0.52 |
| Pakistan | 102 | 101 | 96 | 96 | 96 | 0.60 | 0.40 | 0.49 | 0.81 | 0.50 | 0.56 | 0.55 | 0.57 |
| Lesotho | 103 | 106 | 117 | 114 | 118 | 0.19 | 0.76 | 0.53 | 0.17 | 0.48 | 0.41 | 0.44 | 0.42 |
| Uganda | 104 | 103 | 101 | 101 | 99 | 0.34 | 0.70 | 0.44 | 0.60 | 0.49 | 0.51 | 0.51 | 0.52 |
| Zimbabwe | 105 | 107 | 114 | 111 | 114 | 0.15 | 0.79 | 0.53 | 0.30 | 0.48 | 0.44 | 0.46 | 0.45 |
| Kenya | 106 | 104 | 104 | 104 | 103 | 0.34 | 0.74 | 0.39 | 0.56 | 0.48 | 0.50 | 0.50 | 0.51 |
| Yemen | 107 | 105 | 98 | 98 | 98 | 0.58 | 0.50 | 0.36 | 0.80 | 0.48 | 0.55 | 0.53 | 0.55 |
| Madagascar | 108 | 108 | 107 | 108 | 110 | 0.47 | 0.60 | 0.33 | 0.50 | 0.47 | 0.47 | 0.47 | 0.47 |
| Nigeria | 109 | 110 | 112 | 112 | 112 | 0.44 | 0.59 | 0.36 | 0.43 | 0.46 | 0.46 | 0.46 | 0.46 |
| Mauritania | 110 | 109 | 100 | 105 | 102 | 0.45 | 0.42 | 0.52 | 0.68 | 0.46 | 0.51 | 0.50 | 0.52 |
| Gambia | 111 | 111 | 103 | 106 | 104 | 0.48 | 0.40 | 0.47 | 0.70 | 0.45 | 0.50 | 0.49 | 0.51 |
| Senegal | 112 | 112 | 106 | 109 | 106 | 0.46 | 0.39 | 0.46 | 0.63 | 0.44 | 0.48 | 0.47 | 0.48 |
| Guinea | 113 | 113 | 109 | 110 | 107 | 0.40 | 0.37 | 0.51 | 0.65 | 0.43 | 0.47 | 0.46 | 0.48 |
| Tanzania_U_Rep_of | 114 | 114 | 110 | 113 | 109 | 0.31 | 0.62 | 0.29 | 0.70 | 0.40 | 0.46 | 0.45 | 0.48 |
| Cote_d_Ivoire | 115 | 115 | 116 | 116 | 116 | 0.27 | 0.47 | 0.45 | 0.55 | 0.39 | 0.42 | 0.42 | 0.44 |
| Zambia | 116 | 116 | 121 | 120 | 120 | 0.13 | 0.68 | 0.36 | 0.39 | 0.38 | 0.38 | 0.39 | 0.39 |
| Malawi | 117 | 117 | 119 | 119 | 119 | 0.21 | 0.66 | 0.29 | 0.44 | 0.38 | 0.39 | 0.39 | 0.40 |
| Central_African_Rep | 118 | 118 | 124 | 123 | 124 | 0.25 | 0.43 | 0.41 | 0.21 | 0.36 | 0.33 | 0.34 | 0.33 |
| Ethiopia | 119 | 119 | 111 | 115 | 108 | 0.34 | 0.39 | 0.34 | 0.87 | 0.36 | 0.46 | 0.44 | 0.48 |
| Mozambique | 120 | 121 | 118 | 118 | 117 | 0.22 | 0.45 | 0.39 | 0.67 | 0.35 | 0.41 | 0.41 | 0.43 |
| Guinea-Bissau | 121 | 120 | 120 | 121 | 121 | 0.34 | 0.39 | 0.33 | 0.51 | 0.35 | 0.38 | 0.38 | 0.39 |
| Burundi | 122 | 122 | 115 | 117 | 115 | 0.26 | 0.45 | 0.31 | 0.80 | 0.34 | 0.43 | 0.42 | 0.45 |
| Mali | 123 | 123 | 122 | 122 | 122 | 0.39 | 0.21 | 0.37 | 0.44 | 0.33 | 0.35 | 0.34 | 0.35 |
| Burkina_Faso | 124 | 124 | 123 | 124 | 123 | 0.35 | 0.16 | 0.40 | 0.49 | 0.31 | 0.34 | 0.34 | 0.35 |
| Niger | 125 | 125 | 125 | 125 | 125 | 0.35 | 0.18 | 0.35 | 0.44 | 0.30 | 0.32 | 0.32 | 0.33 |

Source: Sarker et al. (adapted from HDRs of UNDP); PCI is named as GDP in HDR/Sarker et al. $\quad$ Computed by us


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JUNE 112007
DEPARTMENT OF ECONOMICS
NORTH-EASTERN HILL UNIVERSITY, SHILLONG (INDIA)
CONTACT: mishrasknehu@yahoo.com

