Peak-hour Metro Rail Traffic Congestion Alleviation

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Abstract

Dubai Metro is the city railway transport under the Road and Transport Authority (RTA) of Dubai. It is operated as a cyclic schedule on fixed O-D pairs and two lines. The two lines are (i) the Red line which runs between Rashidiya and Jebel Ali and (ii) the Green line which operates between Al Qusias and Creek. Union and Khalid bin Waleed are the two cross-over stations between the two lines. Operational times are based on week days and weekends and the headways are based on peak hour and off-peak hours of the day. Light rails are used in Dubai Metro and each train has five cabins. On both lines, headways are designed at 90 seconds, whereas currently operated headway during peak hours is 3.5 minutes. A high ridership is observed during the last working day and particularly during peak hours, leading to severe over-crowding. To reduce over-crowding and alleviate congestions, three types of strategic solutions are available. (i) Reduce peak hour headways (ii) Increase number of cabins in trains operated during peak hours. (iii) Increase number of services between modified O-D pairs with denser traffic. The problem domain is modeled as a directed transit network and further as an LP formulation with a focus on the third solution for the Red line, under an assumption of known demand. Nodes represent arrival/departure times at each station and two types of arcs represent storage and movement of train cabins, respectively. Constraints on (i) consistency of flow, (ii) non-negativity of flow, (iii) indivisibility, (iv) demand satisfiability and (v) bounds are proposed. The objective has two components: (i) To minimize the number of train cabins in the system and (ii) To minimize the total car miles run by all trains in a schedule cycle. The LP Model developed for the third proposed solution is tested with actual data extracted in September 2012 using an open package LP/MILP IDE for Win32, namely GUSEC. Partial results are obtained and reported. Several interesting questions have arisen out of our model and we are trying to analyze some of them. Attempts continue (i) to acquire, test and evaluate validated data from RTA, (ii) apply the proposed model to green line and study congestion alleviation of red and green lines in a combined manner and (iii) evaluate the model against other possible solutions.

1 Introduction

Dubai Metro is operated as LRT with 5 cabin trains. Currently two lines are operational, namely the red line (54 km) and the green line (23 km). Trains are automatically operated with the Red line running between Rashidiya and Jebel Ali and (ii) the Green line operating between Al Qusias and Creek. Two yards at Rashidiya and Jebel Ali serve the red line trains and one yard at Qusais serves the green line trains. Operational hours are based on days of the week and headways between the trains are based on hours of the day. The entire system is designed to handle a 90 seconds headway, though the peak hour traffic is operated at 3.5 minutes. It is observed that the peak hour demands are very high in both lines and particularly during the week ends. To alleviate congestion, three types of solutions are considered. (i) Reduce peak hour headways (ii) Increase number of cabins in trains operated during peak hours. (iii) Increase number of services between modified O-D pairs with denser traffic. The two lines operate between fixed O-D pairs and peak hour traffic is generally directed at one direction in the morning and the opposite in the evening. For that reason, reducing peak hour headway shall reduce the number of empty runs in the reverse direction and hence is not a favored solution. Increasing the number of cabins in a train shall not be allowed, as some stations are limited in the number of cabins that can be accommodated. Union and Khalid bin Waleed are the two cross-over stations between the two lines. Based on ridership data available over the years, traffic is highest between Deira and Emirates Mall on the red line and between Union and Oud Mehta on the green line. Interestingly peak hour traffic is dense around two bottle neck stations, Deira and Emirates mall on the red line and around Union and Oud Mehta on the green line. The third option is being considered to offer additional services in the bottle neck corridor between additional O-D pairs. At the present level of implementation, only the red line is being tested and evaluated.

2 Problem Statement

Peak-hour traffic between certain stations on the red line and green line lead to enormous congestion and passenger dis-comfort. To alleviate congestion and ease traffic mobility, it is proposed to consider an additional O-D pair on the red line between Deira and Emirates Mall and to operate trains between these corridors with smaller headways during peak hour traffic. The problem is to find out the minimum number of trains required to transport the passengers between the bottle neck stations during peak hours. The objectives proposed to the problem are namely (i) To minimize the number of train cabins in the system and (ii) To minimize the total car miles run by all trains in a schedule cycle under the constraints of (i) consistency of flow, (ii) non-negativity of flow, (iii) indivisibility (iv) demand satisfiability and (v) bounds. It is further assumed that demand during peak hours is known. An LP Model is developed for the third proposed solution and evaluated with actual data extracted from the read line in September 2012 using an open package LP/MILP IDE for Win32, namely GUSEC.



Figure 1: The Redline route between RSA and JBA

3 Formulation of the model

The proposed model is motivated by the railroad network and in this section, the network that applies to the problem statement of Dubai Metro is completely described. A fleet of cabins provides transport service between two fixed O-D pairs on the red and green lines. A set of trains is scheduled on both lines, each comprising 5 cabins each. At any given time, cabins are either part of running trains or stored at one of three yards. Two requirements restrict the size and deployment of cabins, and hence the trains: one is the fixed schedule and second is the known demands for scheduled trains.

- **Fixed Schedule:** It is a list of all trains that depart in a schedule cycle. An entry in the list specifies each city of departure and arrival and the corresponding departure and arrival times. In the congestion alleviation problem of Dubai Metro, we consider the cyclic schedule of red line on Thursdays.
- **Demands:** For each scheduled train, there is a known demand which must be met. A minimum number of cabins is required in each train.

In the following two tables, ridership in the redlines in either directions (Rashidiya to Jebel Ali and Jebel Ali to Rashidiya) are given.

3.1 Ridership details

• September - Red Line

Weekday PPHPD AM Peak- 5408



Figure 2: The modified O-D pairs of Deira and Emirates Mall station

Weekday: Rashidiya to Jebel Ali			
Schedule period	Headways	Number of cabins	
0550 to 0630	7 Minutes	21	
0630 to 0900	3.5 Minutes	41	
0900 to 1530	8 Minutes	18	
1530 to 1740	7 Minutes	21	
1740 to 1900	3.5 Minutes	41	
1900 to 2000	7 Minutes	21	
2000 to 2300	8 Minutes	18	
2300 to 0000	10 Minutes	14	

Weekday: Jebel Ali to Rashidiya			
Schedule period	Headways	Number of cabins	
0550 to 0900	7 Minutes	21	
0900 to 1515	8 Minutes	18	
1515 to 1630	7 Minutes	21	
1630 to 1900	3.5 Minutes	41	
1900 to 2200	8 Minutes	18	
2200 to 0000	10 Minutes	14	

Weekday PPHD PM Peak- 6620 Weekday PPHD off peak - 1800 approx Thursday PPHPD AM Peak -5673

Thursday: Rashidiya to Jebel Ali			
Schedule period	Headways	Number of cabins	
0550 to 0630	7 Minutes	21	
0630 to 0900	3.5 Minutes	41	
0900 to 1530	8 Minutes	18	
1530 to 1740	7 Minutes	21	
1740 to 1900	3.5 Minutes	41	
1900 to 2200	8 Minutes	18	
2000 to 2300	8 Minutes	18	
2300 to 0000	10 Minutes	14	

Thursday: Jebel Ali to Rashidiya			
Schedule period	Headways	Number of cabins	
0550 to 0630	7 Minutes	21	
0630 to 0900	3.5 Minutes	41	
0900 to 1515	8 Minutes	18	
1515 to 1630	7 Minutes	21	
1630 to 2000	3.5 Minutes	41	
2000 to 2300	8 Minutes	18	
2300 to 0000	10 Minutes	14	

Friday: Operational hours		
Schedule period Headways Number of cabins		
1300 to 0100	8 Minutes	18

Saturday: Operational hours		
Schedule period	Headways	Number of cabins
0550 to 0100	8 Minutes	18

Green Line: Week day and Saturday		
Schedule period	Headways	Number of cabins
0500 to 0000	8 Minutes	10

Green Line: Thursday		
Schedule period	Headways	Number of cabins
0550 to 0100	8 Minutes	10

Green Line: Friday		
Schedule period	Headways	Number of cabins
1300 to 0100	8 Minutes	10

Thursday PPHD PM Peak - 7067 Thursday PPHD off peak - 2000 approx Friday PPHPD - 2500 approx Saturday PPHD - 3500 approx

• Green Line

Weekday - 1600 max Thursday - 1600 max Friday - 1400 max Saturday - 1400 max

A total of 79 trains, each with 5 cabins are deployed. A total of 16 trains spares in red line (80 cabin spares on red line) and 5 trains spares on green line (25 cabin spares) are available. We consider the stations, Deira and Emirates Mall stations on the redline and the number of passengers that travelled between the stations in September, 2012.

3.2 Transit network model

We define one node for each city in the network for each time. The schedule period is divided into τ uniform intervals. We have considered $\tau = 144$, which means $T = \{0, 1, 2, ..., 144\}$ and each time interval at every ten minutes is considered. We connect the nodes by arcs of two types, by cabins in storage and cabins in trains. We assume the following in our proposed model.

- Demand at each city (station) and at each interval is known.
- Dedicated tracks are assumed in each direction of train movement.

- No train is allowed to overtake any other train.
- Headway is maintained.
- **Storage arcs:** For each city, run an arc from the node for each time t to the node for the next time, $(t + 1) \mod \tau$. This would give the number of cabins available as storage cabins in the city during that interval at the beginning of t.
- **Train arcs:** For each scheduled train, run an arc from the node representing the city and time of departure to the node for the city and time of arrival. Flow along this arc represents cabins moving from one city to another in the scheduled train.

3.3 Constraints

- **Consistency of flow:** This constraint ensures that the net flow at every node is zero. The number of cabins in storage during interval t at a given city must equal the number in storage in the interval immediately before, plus the number that arrived at time t less the number that departed at t.
- **Non-negativity of flow:** All flows are non-negative. This ensures that trains cannot move backwards in time and space.
- Indivisibility: Cabins are in indivisible units, and hence all flows must be integral.
- **Demand satisfiability:** The flow on each train arc must be greater than or equal to the number of cabins required to meet demands.
- **Bounds:** This constraint limits the maximum and minimum number of cabins in a train. The RTA does not allow flexibility in the number of cabins attached to a train. It is a fixed 5-cabin train, as of now. But as a generic model, it is possible to vary the number of cabins.

3.4 Reducing the network

If no trains arrive or depart city c at time t, the city is connected to the rest of the network by only two storage arcs: an incoming arc from the previous time and outgoing arc to the following time. These flows must be equal to satisfy the consistency of flow constraint. Consequently this arc may be removed and the two arcs may be replaced with one. The redline network is reduced based on the above discussions and the modified O-D pairs are considered. At the present level of implementation, green line is not considered in our computation, though we have illustrated in the figure. IIMA • INDIA

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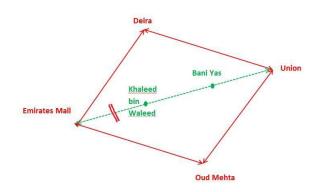


Figure 3: Reduced network model of RSA-JBA on redline

3.5 **LP** Formulation

Notation: The notation of sets and variables used in the proposed model is listed below:

- C: The set of cities; $C = \{A, B, C, D\}$
- T: Set of intervals into which the schedule period is divided; $T = \{0, 1, 2, 3, ... \tau\}$
- S: The known schedule; $S = \{(c, t, c', t') : c \in C, c' \in C, t \in T, t' \in T \text{ and } t \in C, t' \in T, t' \in T \}$ $c \neq c'$

An element in S represents a train that leaves city c at time t and arrives at c' at t'.

- $d_{cc'}{}^{tt'}$: Smallest number of cabins required to meet demand for train (c, t, c', t') $d_{aa'}{}^{tt'} > 0.$
- $h_{cc'}{}^{tt'}$: Maximum number of cabins required to meet demand for train (c, t, c', t') $h_{cc'}{}^{tt'} > 0.$
- $N_c(t)$: Nodes of the network, $\forall c \in C$ and $t \in T$
- AS_c^{t} : Directed arcs that represent storage of unused cabins, $\forall c \in C$ and $t \in T$ $AS_c^t \colon N_c(t) \to N_c((t+1) \mod \tau)$ as_c^t : LP variable that defines train flow over AS_c^t , $\forall c \in C$ and $t \in T$

• $AM_{cc'}{}^{tt'}$: Directed arcs that represent movement of cabins, $\forall c, c' \in C$ and $t, t' \in C$ T

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AM_{cc'}^{tt'} \colon N_c(t) \to N_{c'}(t')
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 $am_{cc'}{}^{tt'}$: LP variable that defines train flow over $AM_{cc'}{}^{tt'}, \, \forall \, c, c' \in C$ and $t,t' \in T$

• $m_{cc'}$: Distance in miles from c to c'

Constraints: The list of constraints in LP notation is given below.

1. Consistency of flow:

$$as_{c}^{(t-1) \mod \tau} + \sum_{(c1,t1,c,t)\in S} am_{c1c}^{t1t} = as_{c}^{t} + \sum_{(c,t,c2,t2)\in S} am_{cc2}^{tt2}, \forall c \in C \text{ and } t \in T$$

For every city and time, unused cabins in the present interval must equal unused cabins in the previous interval, plus cabins just arriving in trains, minus cabins just leaving in trains

2. Non-negativity of flow:

 $as_c^t \geq 0, \forall c \in C \text{ and } t \in T$

Cabins are not permitted to run in the reverse direction.

3. Indivisibility:

 $as_c^{t} \in \{0, 1\}, \forall c \in C \text{ and } t \in T$ $am_{cc'}^{tt'} \in \{0, 1\}, \forall c \in C \text{ and } t \in T$ Cabins are indivisible.

4. Demand satisfiability:

 $am_{cc'}{}^{tt'} \ge d_{cc'}{}^{tt'}, \forall (c, t, c', t') \in S$

For each scheduled train, number of cabins must meet demand, but must not be so great that unnecessary cabins are run.

5. Bounds:

$$\begin{aligned} h^{tt'}_{cc'} &\geq d^{tt'}_{cc'} \\ d^{tt'}_{cc'} &\leq a m^{tt'}_{cc'} \leq h^{tt'}_{cc'} \end{aligned}$$

Minimum and maximum number of cabins are specified for a given demand between cities at a given time interval.

Objective Function: Based on the problem statement and the set of constraints, a feasible set of cabin allocations may be determined for each train in the schedule, if one exists. Here we propose a linear objective function to optimize such an allocation of the train flow variables. A case of two objectives is developed, for a schedule period of one day. A set of solution activities of as_c^{t} and $am_{cc'}^{tt'}$ variables is written as (as, am) and the value

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of the objective function Z at the solution is Z(as, am). Two costs are proposed and the objective is to minimize the total cost. The first cost is fleet cost, directed at minimizing the number of cabins in the fleet. The second cost is the operating cost, directed at minimizing the number of cabin-miles.

Let at t^* , $0 \le t^* \le (\tau - 1)$, the total number of cabins in the system be determined. For a feasible solution, this number must be same at any t^* , since cabins do not enter or leave an operational system. Let us consider, $t^* = \tau - 1$. Then the total number of cabins is given by,

$$Z_{fleet} = \sum_{c \in C} a s_c^{\tau-1} + \sum_{(c,t,c',t') \in S} a m_{cc'}^{tt'}$$

Let $m_{cc'}$ be the distance from c to c'. Then total cabin miles in given by,

$$Z_{mile} = \sum_{(c,t,c',t') \in S} m_{cc'} X a m_{cc'} tt'$$

The objective function is to minimize total cost Z and is given by

$$Minimize \ Z(\mathbf{as}, \mathbf{am}) = p_1 \ X \ Z_{fleet} + p_2 \ X \ Z_{mile}$$

where p_1 and p_2 be the constants of proportionality of the costs Z_{fleet} and Z_{mile} respectively.

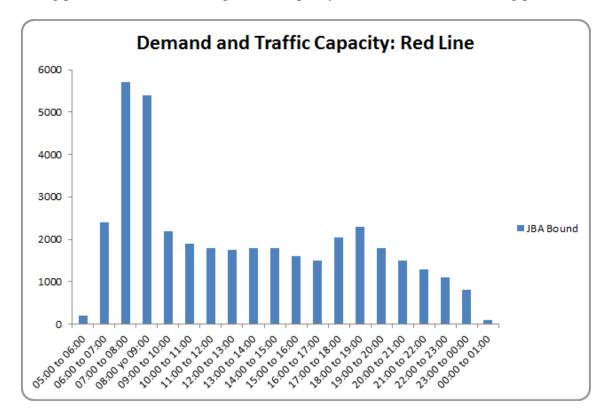
4 Implementation

Dubai Metro operates with fixed O-D pairs, which is Rashidiya (RSA) and Jebel Ali (JBA). To maintain consistency of evaluation, results are compared between the two bottleneck stations, Deira and Emirates Mall stations. The model is implemented and three different variations are reported. (i) Data 1 is the currently operated schedule and demands. (ii) Data 2 is a proposed capacity increase of number of trains run between the given O-D pair, by manually increasing the number of cabins in movements during the peak hour time intervals. (iii) Data 3 is a feasible solution of the model, to determine the number of cabins in movement and storage. Optimality has to verified with more rigorous tests.

4.1 Computations

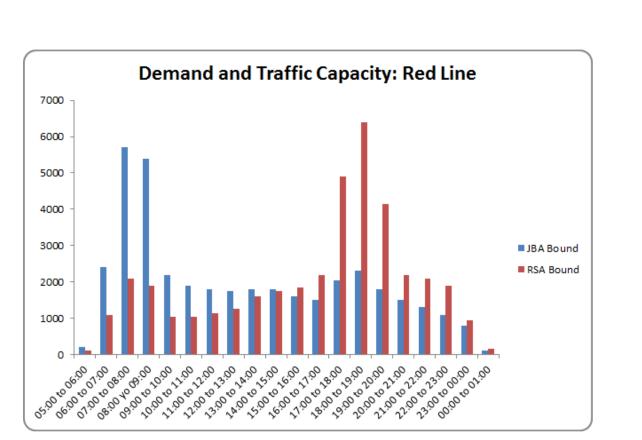
The GUSEC solver was used to solve the LP congestion alleviation model. With the available data of Dubai Metro ridership, the model was implemented between the densest corridor on the

redline, which is Deira - Emirates Mall station. Three instances of experimentation was done with the following variations: (i) The currently operated capacity on the redline; It is observed that line is congested during peak hours. (ii) The second set of data proposes an increased capacity during peak hours by reducing the headways during peak hours. (iii) The third results in the least objective, which is proposes increasing the service capacity towards JBA in the morning peak hours and increasing service capacity towards RSA in the evening peak hours.



5 Summary

We have used tentative values for the two proportionality constants p_1 and p_2 , which needs to be verified. As can be observed, solutions are highly sensitive to the two proportionality constants. Attempts are on to obtain valid test data from RTA and to evaluate results against other comparable results. Further studies are directed towards extending the model to the green line and determining the combined effect of congestion alleviation in both lines together.



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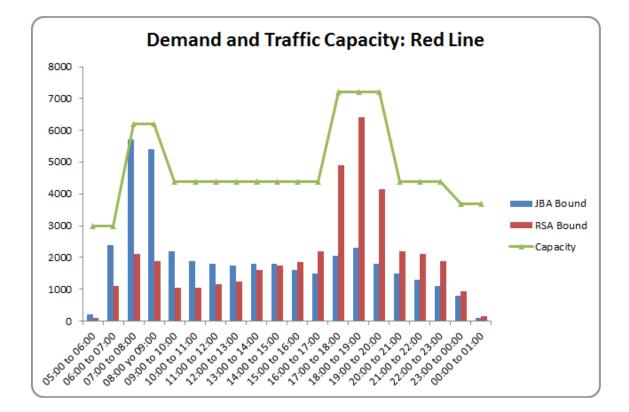


Table 1: Numerical results of Solving the Congestion Alleviation Model

